

# Climate Dynamics

## Simple Climate Models

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### Overview : 4 Lectures

- ◆ 1) Basic facts and findings
  - The global energy balance
  - Zero-dimensional EBM's
- ◆ 2) Introducing latitudinal effects
  - 1D (meridional) EBM's
  - ice/albedo feedback
- ◆ 3) Introducing vertical effects (in the atmosphere)
  - 1D radiative-convective models
- ◆ 4) 2D (meridional & vertical) models
  - statistical-dynamical models
  - the atmosphere
  - the ocean
  - and land ???

## Acknowledgements & materials

- ◆ Developed from MIT course of Peter Stone
  - see Stone (1997)
  - similar content, different presentation
- ◆ Material (and many illustrations) from
  - McGuffie & Henderson-Sellers “A Climate Modelling Primer” (2nd edition, 1996) : £29-95 paperback
  - Trenberth (1992) “Climate System Modelling”
  - Kump, Kasting & Crane (1999) “The Earth System”

## Simple Climate Models

### Lecture 1

Basic facts and findings  
The global energy balance  
Zero-dimensional EBM's

## The Climate System

- ◆ Ocean
- ◆ Atmosphere
- ◆ Cryosphere (both land and sea-ice)
- ◆ Hydrosphere (Evaporation, precipitation, groundwater, rivers...)
- ◆ Biosphere (both terrestrial & marine)
- ◆ Geosphere : tectonics (continental configuration), volcanic dust & CO<sub>2</sub>
- ◆ ... and the *interactions* between them

## Simple Models

- ◆ “Simple” means one or more of ...
- ◆ low dimensional
  - zero, one, two, three (?) ...
  - low order, i.e. coarse resolution
    - up to (say) ~ 30 x 30 x 30...
  - low complexity
    - use parameterisation rather than detailed simulation of complex processes....  
(a higher-order intellectual activity !)

## Simple Models : Types

- ◆ Energy Balance Models
  - may be zero, one or two dimensional
  - model the land/sea surface and its interactions with the rest of the Universe
  - do not really model the atmosphere...
- ◆ Radiative-Convective Models (atmosphere)
  - usually 1D (vertical) :
  - point-wise or global average ?
- ◆ Box models (many variants thereof)
- ◆ Meridional/vertical models (2D)
  - “statistical-dynamical”
  - atmosphere and/or ocean

## The Global Energy Balance

- ◆ At the top of the atmosphere (TOA)..
  - Earth receives incoming Short-wave (UV/Visible) radiation
    - some is reflected (albedo)
  - Earth emits Outgoing Long-wave (thermal infra-red) Radiation (OLWR)
    - Black-body radiation
    - at the effective TOA temperature ( $T_{\text{eff}}$ )
    - NB : atmospheric lapse rates...  $T_{\text{eff}} < T_s$
- ◆ OLWR from surface
  - is perturbed by atmospheric IR absorption & re-emission (the greenhouse effect)

## Incoming Short-wave Radiation

- ◆ Solar Constant :  $S_0 = \sim 1360 \text{ W m}^{-2}$
- ◆ Projected Area of Earth =  $\pi R^2$
- ◆ Surface Area of Earth =  $4 \pi R^2$
- ◆  $\therefore$  Global average insolation  
 $S_{\text{bar}} = S_0 / 4 = 340 \text{ W m}^{-2}$
- ◆ at the equator,  $S_{\text{equ}} = S_0 / \pi = 433 \text{ W m}^{-2}$
- ◆ varies roughly as  $\cos(\theta)$ 
  - but NB effect of obliquity
  - at the poles, if obliquity were zero, S would be zero, and it would be very cold indeed ....

## Climate Forcing

- ◆ “climate forcings” are usually expressed as (vertical) heat fluxes (in  $\text{W m}^{-2}$ )
- ◆ for  $2x\text{CO}_2$ ,  $G_{\text{CO}_2} \approx 4 \text{ W m}^{-2}$
- ◆ for clouds,  $C_{\text{net}} \approx 0 \pm 20 \text{ W m}^{-2}$
- ◆ NB vertical divergences (gradients) of forcing fluxes yield heating rates (e.g. in K per day)
  - if these are non-zero, we have imbalance, and thus non steady-states (or there must be other transports not yet accounted for)

## Albedo

- ◆ Albedo ( $\alpha$ ) = SW reflectivity
  - Water <0.1
  - Vegetation 0.1 to 0.2
  - Bare Land 0.2 to 0.3
  - Clouds ~0.5
  - Ice & snow 0.5 to 0.9
- ◆ Planetary average ~0.3
  - mostly due to clouds (2/3)
  - and snow/ice (1/3)

## Outgoing Long-wave Radiation (OLWR)

- ◆ Stefan-Boltzmann law :  $F = \sigma T^4$ 
  - $\sigma = 5.67 \text{ E}(-8) \text{ W m}^2 \text{ K}^{-4}$
  - $\Rightarrow$  dominant (negative) **feedback**
- ◆ but : IR absorption/emission by the atmosphere
  - transmissivity( = emissivity)  $\epsilon \approx 0.6$
- ◆ causes GH effect : mainly due to water vapour
  - $T_s - T_{\text{eff}} \approx 33 \text{ }^\circ\text{C}$  (or “g” =40%)
- ◆ but vapour pressure increases with temperature & thus transmissivity **decreases** ( $\Rightarrow$  positive feedback)
  - NB : Clausius-Clapeyron relationship
  - $q_s = q_0 \exp(-5420/T)$

## Estimation of OLWR

### ◆ Empirical

- Budyko (1969) : linear relationship
- Sellers (1969) : non-linear relationship
- from satellites (ERBE etc)

### ◆ Theoretical

- 1D radiative convective models
- Pierrehumbert (1995)
- Hartmann & Michelson (1993)

### ◆ Should be somewhat non-linear...

### ◆ Still not very well established ( $\pm 20 \text{ W m}^{-2}$ )

## Budyko's Linear Approximation

### ◆ $F \approx 204 + 2.17 T_s$ ( $\text{W m}^{-2}$ )

- (NB :  $\exists$  various values for the constants)

### ◆ this implies a Climate Sensitivity (with no ice-albedo feedback) of $\lambda = 1/2.17 = 0.46 \text{ K per W m}^{-2}$

### ◆ whereas, for a pure Stefan-Boltzmann black body, $\lambda \approx 0.3 \text{ K per W m}^{-2}$

### ◆ the difference is due to the water vapour greenhouse effect (positive feedback)

## Energy Balance Models

- ◆ Budyko (1969), Sellers (1969)
- ◆ see also North (1975), North et al (1981)
- ◆ Simplest case : zero-dimensional models
  - apply to globally averaged conditions
  - surprisingly successful & useful
    - (if carefully parameterised...)
  - because OLWR is well approximated by a linear function of  $T_s$
  - so OLWR is not dependent on spatial distribution of heat (temperature)

## Globally Averaged EBM

- ◆ For global energy balance :
- ◆  $(1 - \alpha) S_{\text{bar}} = \epsilon \sigma T_s^4$  (Stefan-Boltzmann)
  - where transmissivity  $\epsilon \approx 0.6$
  - albedo  $\alpha \approx 0.3$
  - $S_{\text{bar}} = 340 \text{ W m}^{-2}$
- ◆  $\therefore T_s = \{(1 - \alpha) S_{\text{bar}} / (\epsilon \sigma)\}^{0.25} - 273.2$
- ◆ alternatively....
- ◆  $(1 - \alpha) S_{\text{bar}} = F \approx 204 + 2.17 T_s$  (Budyko)
- ◆  $\therefore T_s = \{(1 - \alpha) S_{\text{bar}} - 204\} / 2.17$



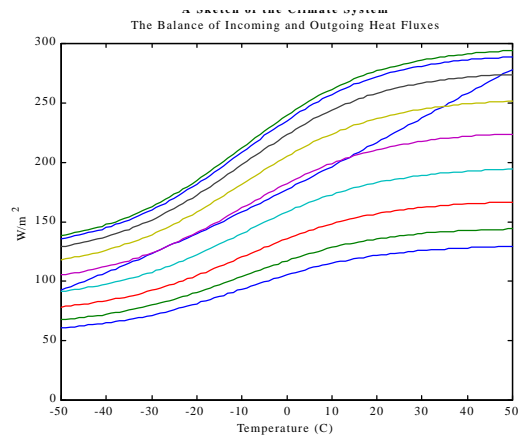
## Global mean temperatures

- ◆ For Budyko' parameterisation, with
  - albedo  $\alpha \approx 0.3$
  - $S_{\text{bar}} = 340 \text{ W m}^{-2}$
- ◆ (and also for S-B with transmissivity  $\epsilon \approx 0.6$ )
- ◆  $T_s \approx 16 \text{ }^\circ\text{C}$
- ◆ For albedo  $> \approx 0.4$ ,  $T_s$  (Budyko)  $< 0 \text{ }^\circ\text{C}$ 
  - ( $\therefore$  ice everywhere ...)
- ◆  $T_s$  (Budyko) varies more than  $T_s$  (S-B)
  - due to water-vapour GH effect (+ve feedback)

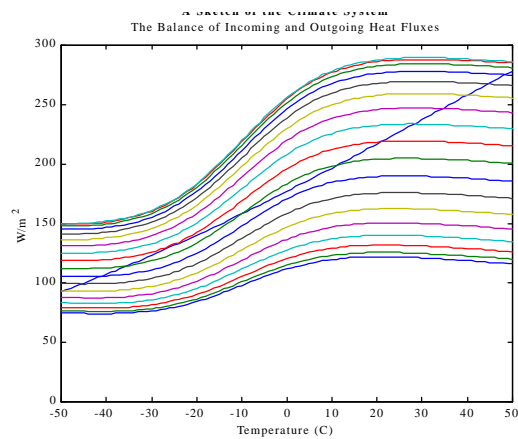
## Ice/albedo feedback

- ◆ for  $T_s > \sim -10 \text{ }^\circ\text{C}$ ,  $\alpha \approx 0.3$
- ◆ for  $T_s < \sim -10 \text{ }^\circ\text{C}$ ,  $\alpha \approx 0.7$
- ◆ approximate by step or logistic function
- ◆ may have multiple stable states
- ◆ possibility of “Snowball Earth”
  - occurred twice ???
    - Huronian and late pre-Cambrian glaciations
    - at circa 2000 and 700 Ma BP

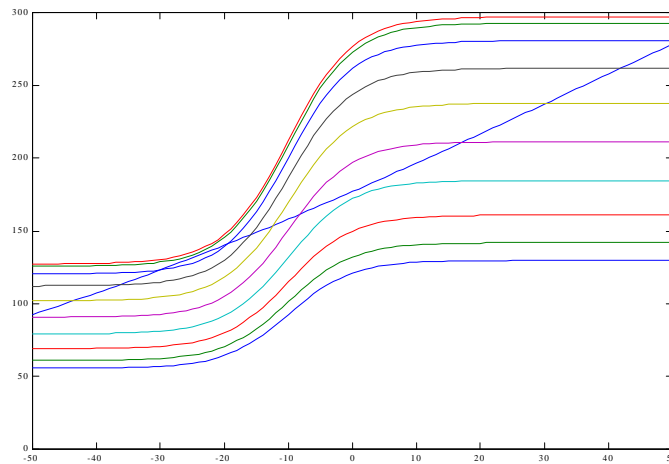
## Effect of Ice-albedo feedback (no mixing)



## Effect of Ice-albedo feedback (with mixing)



Balance between Incoming SW and Outgoing LW Radiation (for various latitudes)  
With Ice/Albedo and Water Vapour Feedbacks (Budyko approximation for OLWR)



## Runaway humid greenhouse ?

- ◆ OLWR has max (capped) at  $\approx 320 \text{ W m}^{-2}$
- ◆ and at the equator...
- ◆  $(1 - \alpha) S_{\text{bar}} \approx 0.7 \times 433 = 303 \text{ W m}^{-2}$
- ◆ if  $S$  increases, or  $\alpha$  decreases, could get runaway humid greenhouse effect
- ◆ the tropics are close to this state, now
- ◆ would continue until all ocean water has boiled (vapour pressure  $\approx 400 \text{ bar}$ ,  $T_s \approx 635 \text{ K}$ ,  $362 \text{ }^\circ\text{C}...$ )
- ◆ has probably occurred on Venus
- ◆ likely for Earth in 1000 Ma (see Kasting 1988)

## Sketch for logistic model

## IR Saturation and the GH Effect

- ◆ If atmosphere is virtually opaque (absorption due to water vapour) why does a bit more absorption due to CO<sub>2</sub> matter ?
- ◆  $T_s = \{(1 - \alpha) S_{\text{bar}} / (\epsilon \sigma)\}^{0.25} - 273.2$
- ◆ but  $\epsilon = \exp(-\tau)$ , where  $\tau$  = optical thickness
  - (proportional to concentration of absorbing substances)
- ∴  $\Delta T_s \propto \exp(\tau/4)$  : increases without limit...
- ◆ NB : continuous (layered) radiative equilibrium calculation  $\Rightarrow \epsilon = 2/(\tau+1)$  (???)
  - Salby, ML, pp88-94 in Trenberth (1992)

## Effects of high & low clouds

## Forcing the system (Climate sensitivities)

- ◆ Values of  $\lambda$  (K per  $\text{W m}^{-2}$ )
  - black body 0.30
  - + water vapour (g-h effect) 0.46
  - + ice-albedo feedback ???
- ◆ Doubling  $\text{CO}_2 \Rightarrow$  forcing  $\approx +4 \text{ W m}^{-2}$ 
  - $\Rightarrow \Delta T \approx 2.5 \text{ }^\circ\text{C}$
- ◆ Ice introduces non-linearity
  - occurs only near the poles
  - must consider spatial variation
  - $\Rightarrow$  need at least a 1D (meridional) model...